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UNCERTAINTY IN SCATTEROMETER-DERIVED VORTICITY

By

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ABSTRACT

A more versatile and robust technique is developed for determining area averaged surface vorticity based on vector winds from the SeaWinds scatterometer on the QuikSCAT satellite. This improved technique is discussed in detail and compared to two previous studies by Sharp et al. (2002) and Gierach et al. (2007) that focused on early development of tropical systems. The error characteristics of the technique are examined in detail. Specifically, three independent sources of error are explored: random observational error, truncation error and representation error. Observational errors are due to random errors in the wind observations, and determined as a worst-case estimate as a function of averaging spatial scale. The observational uncertainty in vorticity averaged for a roughly circular shape with a 100 km diameter, expressed as one standard deviation, is approximately $0.5 \times 10^{-5} \text{ s}^{-1}$ for the methodology described herein. Truncation error is associated with the assumption of linear changes between wind vectors. For accurate results, it must be estimated on a case-by-case basis. An attempt is made to determine a lower bound of truncation errors through the use of composites of tropical disturbances. This lower bound is calculated as 10^{-7} s^{-1} for the composites, which is relatively small compared to the tropical disturbance detection threshold set at $5 \times 10^{-5} \text{ s}^{-1}$, used in an earlier study. However, in more realistic conditions, uncertainty related to truncation errors is much larger than observational uncertainty. The third type of error discussed is due to the size of the area being averaged. If the wind vectors associated with a vorticity maximum are inside the perimeter of this area (away from the edges), it will be missed. This type of error is analogous to over-smoothing. Tropical and sub-tropical low pressure systems from three months of QuikSCAT observations are used to examine this error. This results in a bias of approximately $1.5 \times 10^{-5} \text{ s}^{-1}$ for area averaged vorticity calculated on a 100 km scale compared to vorticity calculated on a 25 km scale. The discussion of these errors will benefit future projects of this nature as well as future satellite missions.

CHAPTER 1

INTRODUCTION

The development of tropical systems has been a widely discussed process for centuries. Accurate, early, prediction of the development of these systems has broad implications for human preparedness. Early research started with the use of surface and upper air data to create composites of developing and non-developing tropical systems (Yanai 1968 and McBride and Zehr 1981). These data were extremely limited, thus restrictive to their storm composites.

There have been many improvements in observations used for tropical storm analysis and tracking in the last five decades. These improvements are greatly attributed to the development of weather satellites. For example, gridded analysis and infrared (IR) satellite data have been used broadly to categorize observed western North Pacific genesis cases according to the prominent large-scale flow pattern (Ritchie and Holland 1999).

The first Geostationary Operational Environmental Satellite (GOES) was launched on Oct. 16, 1975. Data from GOES was used to study easterly waves in the Atlantic basin (e.g., Kossin 2002, Velden et al. 1998, Goerss et al. 1998). In the Atlantic Basin, it was determined that these easterly waves (Carlson 1969; Burpee 1972, 1974, 1975; Reed et al. 1977; Thorncroft and Hoskins 1994 a,b) are related to approximately 63% of tropical cyclones (Avila and Pasch 1992).

Recent observations of easterly waves suggest a genesis process in which mesoscale vortices that are generated within the environment of the easterly wave interact and organize to form the cyclonic surface circulation (Reasor et al. 2005, Ritchie and Holland 1997; Simpson et al. 1997). Surface vector winds as measured by the NASA Scatterometer (NSCAT) aboard the Advanced Earth Observing Satellite (ADEOS) launched on August 16, 1996 led to studies of tropical cyclone genesis. The introduction of QuikSCAT's SeaWinds instrument, launched on June 19, 1999, extensively improved data coverage and availability of ocean surface wind measurements. These new data facilitated research into the potential for earlier identification of likely precursors to tropical depressions (TD), as investigated by Katsaros et al. (2001) and studies (Sharp et al. 2002; Gierach et al. 2007), that directly influenced the research conducted herein.

Sharp et al. (2002) developed an objective technique that could potentially be used operationally to identify systems (depressions and disturbances) likely to develop into tropical storms (TS) or hurricanes. Gierach et al. (2007) modified the method developed by Sharp et al. (2002), and applied it in conjunction with GOES IR to track tropical disturbances much farther back in time than aforementioned methods. They found that convection and surface rotation were both found at the earliest identifiable stages of genesis. A critical component of these studies is the use of near surface winds to examine circulation or rotation.

The main goals of this project are to improve upon the scatterometer-based calculation of area averaged vorticity (referred to from this point as “vorticity”) and to characterize errors in this technique. The major sources of error in the calculation of scatterometer-based surface vorticity are investigated and discussed. The strengths and weaknesses of the new and old methods (that focused on tropical systems) are discussed in terms of the improvements made upon earlier methods, as well as considerations of how accuracy might change for prospective satellite missions.

This paper is organized as follows: Chapter 2 describes the QuikSCAT SeaWinds data used in this study. Details regarding the methodology of the satellite-based vorticity calculation and comparisons to previous techniques are highlighted in Chapter 3. Sources of error including ambiguity selection errors, random vector component errors, truncation errors and representation errors are discussed in Chapter 4. Chapter 5 covers opportunities for improvement for future applications. Overall, the detection technique continues to prove successful while reducing error in the results.

CHAPTER 2

SEAWINDS DATA

The QuikSCAT SeaWinds Scatterometer data set used in this study is an updated version similar to that used by Gierach et al. (2007); version-3a of the Ku2001 product developed by Remote Sensing Systems (RSS). The data set includes time, location, surface (10 m elevation) equivalent neutral wind speed (Ross et al. 1985), wind direction and a rain flag. Four satellite microwave radiometers are used to determine if rain is present at the location of the QuikSCAT observation and when no radiometer data are available, the occurrence of adverse influences from rain is statistically estimated from the scatterometer backscatter (Mears et al. 2000). This use of the rain flagging information is highly conservative. For tropical applications, a conservative rain flag appears to be necessary. However, this approach seriously over-flags in mid-latitude applications.

A limitation on the study of tropical development is the temporal sampling frequency, which is slightly less than twice daily over the Atlantic basin. In contrast, sampling is much better near the ice caps. Unfortunately, cyclones tend to propagate very rapidly in these regions. Another key limitation in the calculation of surface vorticity is the spatial grid. QuikSCAT observations have a 25 km grid spacing within a swath that is 1800 km wide (76 vector wind cells across the swath). Therefore, the smallest spatial scale for which vorticity can be calculated is 625 km^2 , assuming that the spatial resolution is approximately a point. The actual scatterometer wind cell resolution depends on the processing technique used to convert the observed backscatter to wind vectors; however, it is smaller than the grid spacing (Bourassa et al. 2003).

One other limiting factor is degradation of the accuracy of the wind vectors when too large a fraction of the signal returned to the satellite is due to rain (Draper and Long 2004; Weissman et al. 2003, Weissman and Bourassa 2001). The vorticity signatures of tropical systems are often associated with rain; therefore, it is important to develop a technique that is either insensitive to seriously rain contaminated data, or (in this case) attempts to avoid using such data.

The domain for this study is the portion of the Atlantic basin from the western coast of Africa to the east coast of North America and the Equator to 30° N . Utilizing this area of the

basin allows for most Atlantic tropical systems to be detected as well as limiting interference with mid-latitude storm systems. This method for determining vorticity can be applied to any basin; however, the detection thresholds for tropical disturbances determined by Gierach et al. (2007) might require some modification.

CHAPTER 3

METHODOLOGIES

Section 3.1 describes the technique used to calculate vorticity over a range of spatial scales. Section 3.2 puts this technique in the context of previous techniques used to identify tropical systems. The smoothing required for this approach is much different than required for two previous techniques which are described in Sections 3.3 and 3.4.

3.1 Vorticity Calculation

Working with QuikSCAT swath data poses several issues in performing an area averaged vorticity calculation. Swaths are not in a perfectly gridded format and some data points might be missing (due to land contamination or being outside the observational swath) or rain contaminated. To account for this, the calculation technique is developed to work around such points and outputs a missing value if there are insufficient good data points.

Area averaged vorticity (ζ) is calculated at the center of a “shape”, as defined by available data in the swath, using the circulation (C) about the shape and divided by the area (A) of the shape.

$$\zeta = \frac{C}{A} \quad (1)$$

The circulation theorem is used to calculate the circulation:

$$C = \oint \mathbf{v} \cdot d\mathbf{l}, \quad (2)$$

where \mathbf{v} is the velocity along the closed contour and \mathbf{l} is an element tangent to the contour. The wind vector components are linearly interpolated between adjacent good observations: the shape about which the circulation is calculated becomes a series of straight segments. Then $\int \mathbf{v} \cdot d\mathbf{l}$

becomes $\sum_{i=1}^n \mathbf{v}_i \cdot \mathbf{l}_i$, where i represents the segments from one to n . An individual dot product in

this sum can be calculated as

$$\mathbf{v} \cdot \mathbf{l} = \frac{1}{2} (u_{i+1} + u_i, v_{i+1} + v_i) \cdot (x_{i+1} - x_i, y_{i+1} - y_i), \quad (3)$$

where x and y refer to the longitudinal and latitudinal positions (with differences in meters) and u and v are the zonal and meridional components of the surface wind vector. The circulation is the sum of (3), spanning the circumference of the shape.

If the shape is based on only three wind observations, the area (a triangle) is calculated using

$$A = 0.5[(x_2 - x_1)(y_3 - y_1) - (x_3 - x_1)(y_2 - y_1)]. \quad (4)$$

If four or more points are available, area and vorticity are calculated for a polygon using

$$A = 0.5 \left| \sum_{m=2}^{n-1} [A_0 + x_m (y_{m+1} - y_{m-1})] \right|, \quad \text{and} \quad (5)$$

$$A_0 = x_1 (y_2 - y_1) + x_n (y_1 - y_n), \quad (6)$$

where n is the total number of points enclosing the polygon and the values of x and y are determined relative to the center of mass of the points used in the calculation.

The vorticity is then determined using the circulation from equation (3) and the area from equations (4, 5, 6). If more than 20% of the vectors on the circumference of the shape are missing (or more than 25% when only four points are considered), the vorticity is also set to “missing”.

3.2 Detection Technique

The tropical disturbance detection method is vorticity-based, with the relative area averaged vorticity calculated within the QuikSCAT swath. Vorticity is first calculated for a ‘ring’ with a diameter of 100 km (termed here on as “ringsize 4”), or four QuikSCAT cells in diameter (Figure 1). At each vorticity point, a test with four components is conducted.

- 1) The vorticity must exceed a minimum threshold of $5 \times 10^{-5} \text{ s}^{-1}$ as determined by Gierach et al. (2007).
- 2) The maximum non-rain flagged wind speed within and on all sides of the ring must exceed 6.3 m s^{-1} (Gierach et al. 2007).
- 3) The above criteria must be met for at least 30% of the vorticity points within an area with a diameter equal to the diameter used to calculate the vorticity. The area must be centered on the ‘center of mass’ of the observations used in the vorticity

calculation. Typically, this area is equivalent to the points on and within the shape used to calculate the vorticity.

- 4) The 3rd condition must be met within 175 km of the center of a cloud cluster center.

The first and second criteria were not altered for this study but may require fine tuning depending on the application of this method (i.e. tropical system detection or tracking, mid-latitude storm analysis, the basin of interest, etc.). The third point is important for reducing false alarms associated with questionable wind vectors: vectors that should have been flagged as seriously rain contaminated or vectors with large directional errors. Once the locations where the first two criteria are met are determined, the third criterion is examined at these locations and all locations within two grid points. Initially, the third criterion is applied for a ringsize 10 (250 km).

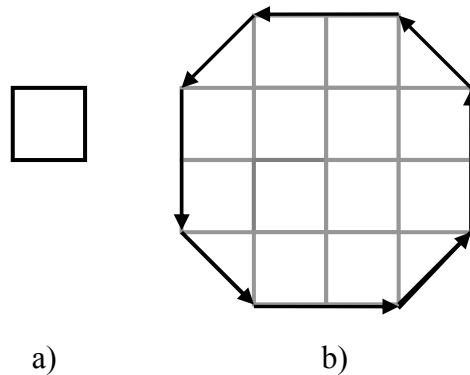


Figure 1. a) Illustration of a ringsize of 1 (utilized by Sharp et al. 2002 and Gierach et al. 2007) that represents an area 25 km by 25 km or one QuikSCAT cell and b) illustrates a ringsize of 4 (used in this study) and represents an area 100 km by 100 km or four QuikSCAT cells. For the previous studies (Sharp et al. 2002 and Gierach et al. 2007), vorticity was calculated from wind vectors at the four corners of the box. In the present study, the number of wind vector data points around the perimeter of the ring is increased and can include as many as 12 data points.

The larger spatial scale improves the identification of systems that are too rain contaminated at a ringsize 4 (100 km scale): e.g., tropical disturbances nearing the tropical depression stage or centers of stronger systems. If a tropical system is not identified at a ringsize 10, the ringsize is decreased by one (diameter is reduced by 25 km), and the process is repeated until all three conditions are met or the diameter reaches a size of zero. If all three criteria are met with a test ringsize greater than zero, the location is noted as being associated with a tropical system.

3.3 Detection technique developed by Sharp et al. (2002)

Sharp et al. (2002) created the foundation for the research of this study by developing an objective technique that could potentially be used operationally to detect storm systems in the tropical disturbance or tropical depression stage of development, that were likely to develop to TS status or higher. That initial study used SeaWinds observations from the 1999 Atlantic hurricane season and included the Gulf of Mexico, the Caribbean Sea and the tropical Atlantic Ocean between 10° N and 25° N.

The key differences from the technique described in Section 3.2 are in the calculation of area averaged vorticity and in smoothing. The spatial scale for Sharp et al.'s vorticity was a 7 by 7 box of scatterometer cells (175 km by 175 km) centered on each vector wind cell in the swath. In practice, the circulation theorem was used to determine the circulation around each 25 km by 25 km box (a square of four adjacent wind vectors) and each of these circulations was then divided by the appropriate area. A minimum of three wind vectors were required for this calculation (a triangle replaces the box). The vorticity was then averaged within the 175 km by 175 km box, which is similar to the total of the circulations divided by the total of the area. Rain flags were not removed due to smoothing associated with spatial averaging. In order for an average vorticity to be calculated from the individual vorticity values, it was required that at least 90% of the vorticity calculations within the 7 by 7 box be valid (non-missing). Next, a similar test containing three criteria was conducted:

- 1) The average vorticity in the 7 by 7 box must exceed $10 \times 10^{-5} \text{ s}^{-1}$.
- 2) The maximum rain-free wind speed within the box must exceed 10 m s^{-1} .
- 3) The above two criteria must be met at least 25 times within a 350 km by 350 km area centered on the center of circulation.

A serious problem with this technique is that circulation about missing points in the interior also contributed to the estimate of circulation. Consequently, even seriously rain contaminated vectors were used in the vorticity calculation in an attempt to eliminate rain contamination as a cause of missing vectors. The center of circulation of the systems detected could be no closer to the edge of a swath or a landmass than 150 km. Sharp et al. (2002) determined that this method of detection proved to be successful for both the 1999 and 2000 hurricane seasons and concluded that future operational use might prove beneficial when used in conjunction with traditional methods. Our new technique, applied with only a radius of 175 km, would likely be a more robust calculation since neither interior circulations nor rain flagged vectors contribute to the total and the land proximity constraint can be dropped.

3.4 Detection technique modified by Gierach et al. (2007)

Gierach et al. (2007) adapted the method developed by Sharp et al. (2002) and coupled it with GOES IR to track storms during the tropical disturbance stage of development. The technique used by Gierach et al. (2007) averages vorticity within SeaWinds swaths in a 100 km by 100 km area. Area averaged vorticity values are calculated using the same technique developed by Sharp et al. (2002). Once vorticity is calculated, a similar, but updated, test of four criteria was conducted:

- 1) The average vorticity in the 100 km by 100 km area must exceed $5 \times 10^{-5} \text{ s}^{-1}$.
- 2) The maximum rain-free wind speed within the box must exceed 6.3 m s^{-1} .
- 3) In a second pass through the data, the above two criteria must be met in at least 80 % of the calculated vorticity cells within 50 km of the vorticity points being tested.
- 4) The 3rd condition must be met within 175 km of the center of a cloud cluster.

Gierach et al. (2007) determined the vorticity and wind speed thresholds, listed above, based on SeaWinds data from the 1999-2004 Atlantic hurricane seasons. Fifteen storms were chosen because they stemmed from African Easterly Waves (AEW). Each storm developed into either a TS or hurricane, providing a point of reference for tracking their development back in time. GOES IR data were used to monitor these storms during times between QuikSCAT overpasses, allowing for a more accurate tracking technique than was possible from either QuikSCAT or

GOES alone. The updated technique, discussed in Section 3.2, is an improvement over Gierach et al.'s technique for the same reasons it is an improvement over the Sharp et al. technique.

CHAPTER 4

DISCUSSION OF ERROR

The important sources of error in our methodology stem from (1) observational errors, (2) truncation errors associated with linear interpolation between wind vectors and (3) mismatches in the spatial averaging scale. It will be shown that the random errors in the area averaged vorticity decrease as the ringsize increases, but the rate of reduction is relatively small for ringsizes greater than 4 (a diameter of 100 km). It will also be shown that estimating truncation error through the use of storm composites as developed by Minter et al. (2007) results in a relatively small truncation error. Finally, it is determined that for vorticity in pre-tropical disturbances or depressions, the bias (relative to a ringsize 1) associated with the spatial averaging scale increases with increasing ringsize.

4.1 Contributions From Observational Errors

Observational errors are due to (a) random vector component errors and (b) ambiguity selection errors. Random errors for SeaWinds on QuikSCAT have been assessed through a variety of approaches (Freilich 1997; Stoffelen 1998; Bourassa et al. 2003; Freilich and Vanhoff 2003). These studies typically investigate the random error where there was no gross error in direction related to ambiguity selection.

4.1.1 Random Errors Ignoring Ambiguity Selection

The propagation of Gaussian distributed random errors can be used to estimate the contribution of observational errors to uncertainty (expressed as a standard deviation) in area averaged vorticity. For a variable (y) that is a function (f) of one or more independent variables (x_i), this function can be described in very general terms as

$$y = f(x_1, x_2, x_3 \dots). \quad (7)$$

The uncertainty in y (σ_y) can be determined (Equation 8) in terms of the uncertainty in the input variables (x_i), again expressed as standard deviations (Taylor 1982).

$$\sigma_y^2 = \left(\frac{df}{dy} \sigma_{x_1} \right)^2 + \left(\frac{df}{dy} \sigma_{x_2} \right)^2 + \dots \quad (8)$$

Assuming the area (A) is determined with negligible error (in a percentage sense), as is the random error in distance (ℓ) between the center of footprints, the uncertainty in the vorticity (σ_z) can be calculated as

$$\sigma_z^2 = \frac{1}{A^2} \sigma_c^2. \quad (9)$$

The uncertainty in circulation (σ_c) is

$$\sigma_c^2 = \sum_{i=1}^n (\ell_i \sigma_u)^2, \quad (10)$$

where σ_u is the uncertainty in the wind speed, assumed to be 0.6 m s^{-1} . Estimates of random component errors for rain-free, correctly selected ambiguities, may be as large as 0.6 m s^{-1} (Freilich et al. 1997) for maximum differences in collocation of 30 minutes and 25 km. Estimates may plausibly be as low as 0.03 m s^{-1} (Bourassa et al. 2003) for collocation differences less than 0.5 minutes and 5 km. Assuming the highest error in vector components provides an upper limit for uncertainty in the vorticity and therefore represents a worst-case scenario. The accuracy is not uniform across the swath; however, since the chosen value includes uncertainty in the comparison data and differences due to mismatches in location and time, it is reasonable to treat it as a constant upper limit.

$$\sigma_c^2 = \sigma_u^2 \sum_{i=1}^{n \leq} l_i^2 \quad (11)$$

Consequently,

$$\sigma_c^2 = \sigma_u^2 \Delta x (n_1 + 2n_2), \quad (12)$$

where n_1 represents the number of “non-diagonal” components of the area perimeter and n_2 represents the number of “diagonal” components of the area perimeter (Figure 1). The length of the diagonal components is the square root of two times the distance (Δx) between the across swath or along swath cells (which is close to constant).

This analysis shows that as ringsize increases, vorticity uncertainty decreases (Figure 2) roughly inversely proportional to the diameter of the area used to calculate the vorticity. For diameters exceeding four grid cells, the decrease in uncertainty is small. Thus, choosing a ringsize larger than 4 would result in only slightly lower levels of uncertainty and would negatively affect the detection technique’s ability to maintain the integrity of smaller scale systems.

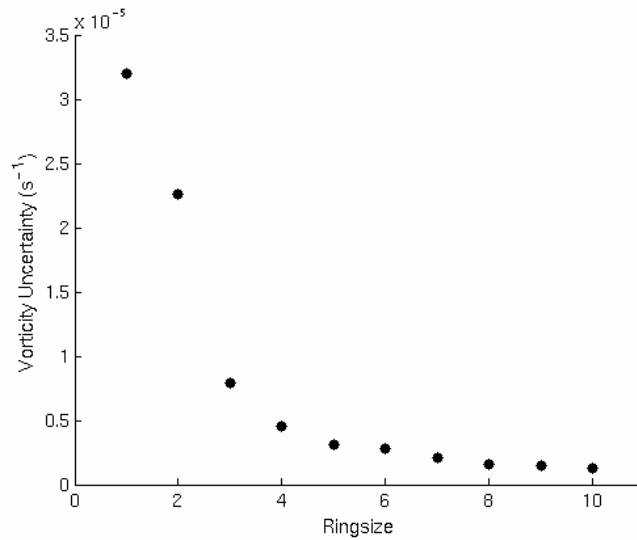


Figure 2. Vorticity uncertainty (s^{-1} , representing one standard deviation) as a function of ringsize. In this study, a ringsize of 4 is used as error is dramatically reduced while preserving the ability to detect small scale systems. In the two preceding studies by Sharp et al. (2002) and Gierach et al. (2007), a ringsize of 1 was used with a great deal of additional smoothing.

4.1.2 Ambiguity Selection Error

Ambiguity selection errors are errors associated with selecting the wrong local minimum in the best fit of a wind vector to observed backscatter (Naderi et al. 1991, Bourassa et al. 2003). The likelihood of an ambiguity selection error is a function of wind speed: it is highly unlikely for wind speeds greater than 8 m s^{-1} and increases as the wind speed decreases below 8 m s^{-1} (for the RSS product). This model of error suggests that the standard deviation of errors in vorticity might be relatively large for low wind speeds. However, it has also been argued that this dependency on wind speed can be largely explained in terms of random errors in wind vector components, where characterization of these random errors is not a function of wind speed (Freilich 1997). That model for observational errors in wind vectors results in vorticity error characteristics that are independent of wind speed.

If ambiguity errors make a substantial contribution to observational errors, then the observational error will increase as the wind speed decreases below 8 m s^{-1} . This dependency on wind speed is examined to determine if there is a substantial contribution from ambiguity errors.

The root mean square differences (RMSDs) of vorticity are calculated, where the difference is the vorticity at a ringsize (from 1–9) and the vorticity for ringsize 10. A ringsize 10 has a greater ratio of wind vectors with correctly selected ambiguities versus ambiguity errors, as well as a larger spatial area (diameter of 250 km). Both considerations reduce the influence of ambiguity errors in the vorticity calculation. For each ringsize, wind speeds from 0 m s⁻¹ to 20 m s⁻¹ are binned in increments of 1 m s⁻¹, and the values in these bins are used to calculate the RMSDs. These RMSDs are examined (Figure 3) to determine if there is an increase in ambiguity selection error as the wind speed decreases below 8 m s⁻¹. There is no evidence of a wind speed dependency. This indicates that ambiguity selection errors are, at most, a weak source of observational error in the vorticity or that observational error is negligible compared to truncation error (discussed in the next section).

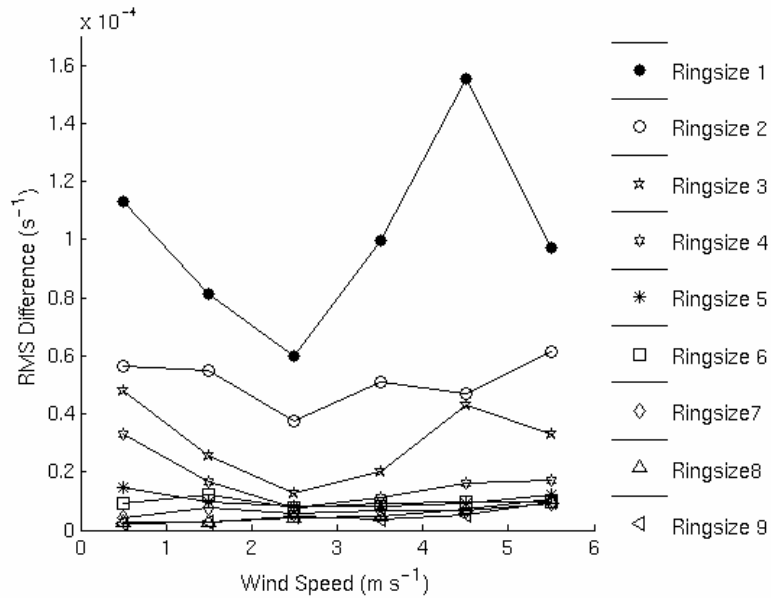


Figure 3. Root mean square error difference versus wind speed (m s⁻¹) for ringsize (i) – ringsize (10). Higher error was expected at low wind speeds if ambiguity selection errors make a substantial contribution to observational errors; however, the results indicate no such trend.

4.2 Truncation Error

The term “ring” is used somewhat loosely, as wind vector spacing only allows a roughly circular shape (Figure 1) composed of a series of straight edges. An assumption is made that the wind speeds change linearly along the segments of the ring. The error in this assumption is related to higher order changes and the grid spacing. The actual changes of wind speed along the segment can be substantially non-linear; for example, centers of strong low pressure systems or poorly organized tropical disturbances. The shape of tropical disturbances varies greatly system by system as well as in time. There are also problems associated with seriously rain contaminated data that are not rain flagged. Furthermore, if some points in the ring perimeter are considered bad points (e.g., land or seriously rain contaminated), then there will be an atypically long line segment joining the neighboring points. This situation can greatly increase truncation errors.

Truncation error associated with the assumption of linear changes between wind vectors is complicated, thus for accurate results, it must be estimated on a case-by-case basis. A lower limit on the value of truncation error is determined by examining truncation error based on composite fields of tropical disturbances. The composites, developed by Minter et al. (2007), are much smoother than individual storms that occur in nature. The composites were split into nine stages of development, where the first was essentially a tropical wave and the last was a TD. Individual storms were based on a blend of QuikSCAT and National Center for Environmental Prediction (NCEP) numerical model analyses. A version of the blending algorithm (adapted from Pegen et al. 2000) was modified for use with NCEP2 reanalysis (Morey et al. 2005; Minter et al. 2007) and constructed with a 1/8 degree grid spacing. Ringsizes from 1 to 4 (diameters of 25 km to 100 km) are examined with the QuikSCAT grid spacing of 25 km and simulated grid spacing of 12.5 km, 8 1/3 km, and 6.25 km (25 times 1, 1/2, 1/3, and 1/4). These grid locations were determined by interpolating between the locations of QuikSCAT wind vectors. Differences are taken between matching points (the locations matching points on the 25 km grid).

The above approach to estimating truncation error results in a rather small random error for the composite disturbance field. The values are approximately 10^{-7} s^{-1} for a single standard deviation of random errors, which is an order of magnitude less than the estimated observational errors. For real world examples (which contain much less smooth fields), it can be assumed that

the errors will be considerably larger, but at this time it is very difficult to assess how much larger.

Assuming that the error statistics are approximately the same for each segment along the edges of the shape (be it a triangle, square or polygon), the total variance associated with random errors in the circulation around the shape (σ_c^2) is approximately proportional to the number of segments times the square of the truncation error uncertainty squared (σ_T^2) of each segment. The number of segments is approximated as the number of points (πn) for a perimeter of a circle associated with a ringsize n .

$$\sigma_c^2 = \sigma_T^2 \pi n \quad (13)$$

It is also assumed that the error associated with the area calculation is considerably smaller as compared to the magnitude of the error in the circulation, and is ignored. The uncertainty in vorticity (σ_ζ) associated with truncation errors is then equal to the uncertainty in circulation divided by the area about which the circulation is calculated. If Δx is the grid spacing of the vector wind observations, then the uncertainty has the following functional form:

$$\sigma_\zeta = \frac{\sigma_T (\pi \cdot n)^{0.5}}{\pi \Delta x^2 n^2 / 4}. \quad (14)$$

The uncertainty related to truncation error is roughly proportional to the square of the length of each segment, which is roughly proportional to $(\Delta x)^2$. Therefore, σ_ζ is proportional to $n^{-1.5}$, seemingly independent of grid spacing within the swath. However, recall that for a constant diameter (averaging area), n is a function of the grid spacing. For any set diameter expressed as a distance (e.g., 100 km), $n\Delta x$ will be constant, hence σ_ζ for a specific spatial scale is proportional to $(\Delta x)^2$: finer grid spacing will greatly reduce truncation errors.

4.3 Representation Error

Spatial averaging errors come in to play when the wind vectors associated with an area averaged vorticity maximum are within the ring used in the vorticity calculations. The larger the ringsize, the more potential there is for a localized vorticity maximum to be missed. In the case of cyclonic systems, representation error tends to result in a negative bias (an underestimation of positive vorticity).

Tropical disturbances from 01 August 1999 through 31 October 1999 were examined to estimate the bias and random errors associated with representation errors. These are systems

typical of our applications. The bias (Figure 4) shows the change in vorticity (centered at the same point) relative to the vorticity for a ringsize 1 (diameter of 25 km). The bias increases as ringsize increases, with a bias of approximately $1.5 \times 10^{-5} \text{ s}^{-1}$ for a ringsize 4 (diameter of 100 km). The magnitude of the bias doesn't decrease much beyond a ringsize 4, thus choosing a ringsize higher than 4 would not drastically improve the bias from this area assumption for this application. The bias typical of tropical disturbances and TDs ($1.5 \times 10^{-5} \text{ s}^{-1}$) doesn't largely impact the application of finding tropical disturbances, since the detection threshold is more than three times larger ($5 \times 10^{-5} \text{ s}^{-1}$). Different biases will be typical of other types of weather (e.g., fronts or high pressure systems) and therefore the shown biases should not be assumed to apply to all situations.

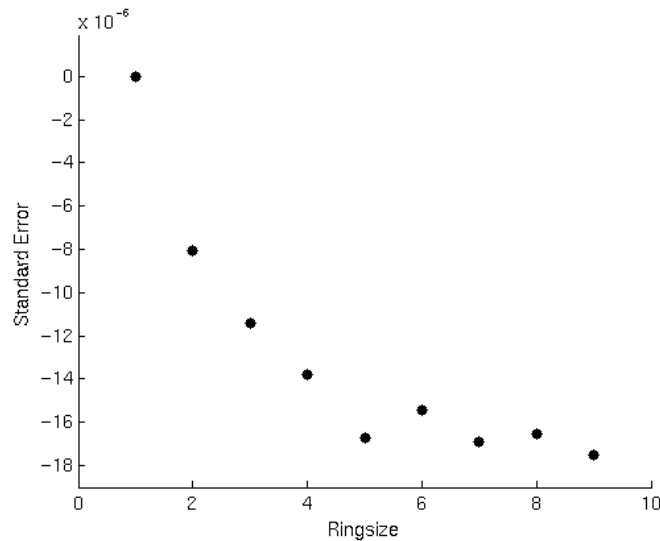


Figure 4. Plot of ringsize (i) – ringsize (1) illustrating spatial averaging scale biases. As the ringsize increases, the area over which the vorticity is averaged increases. This enlargement in area enhances the bias in the vorticity by “smoothing” possible vorticity maxima as shown above.

CHAPTER 5

OPPORTUNITIES FOR IMPROVEMENT AND APPLICATION

As indicated in Chapter 4, errors in the SeaWinds dataset and approximations due to characteristics of the dataset (e.g., grid spacing), are important considerations when dealing with applications that are sensitive to these errors. Improvements in related satellite technology could do wonders for future applications of this technique. The original scope of the project that supported this work was to improve the calculated scatterometer-derived area averaged vorticity, increase the understanding of tropical cyclone genesis or lack of genesis. With improved technology, this detection technique has the potential to contribute to longer tracking times (identification at an early stage) with fewer errors.

One of the greatest changes is improved temporal sampling due to multiple scatterometers in orbit (currently QuikSCAT and ASCAT, with the Indian scatterometer on OCEANSAT2 expected soon). ASCAT's greatly reduced rain contamination (due to the use of C-Band rather than Ku-band) is likely to be a substantial advantage; however, this is offset by somewhat reduced resolution.

Increased resolution and finer grid spacing (and reduced sensitivity to rain), such as is proposed in the eXtended Ocean Vector Wind Mission (XOVWM), would allow for reductions in truncation error in comparison to calculation with a similar trial diameter. The finer spatial resolution should also result in better estimates of random observational errors, due to close collocations, which will also reduce our overestimation of the observational errors. Alternatively, the trial storm diameter could be reduced (without increasing noise), to provide significant decreases in biases (representation errors). The choice tradeoff between reduced bias and reduced random errors would depend on the specifics of the application. For example, the application of forecasting transition to named storms (Sharp et al. 2002) has different requirements than the early detection of tropical disturbances (Gierach et al. 2007). The method developed by Sharp et al. (2002) might not benefit from smaller spatial scales since this would increase random errors, whereas the reduction of noise in larger scale estimates might make the forecasts more accurate.

CHAPTER 6

CONCLUSION

The improved calculation of scatterometer-based area averaged vorticity developed herein can be used for tropical system detection, such as those demonstrated by Sharp et al. (2002) and Gierach et al. (2007), as well as studies of vorticity at other latitudes. Improvements include a more accurate calculation of area, a better handling of missing data (due to rain contamination flags, land, and swath edges), characterization of the key sources of error and a great decrease in the processing time. An understanding of the trade-offs between averaging area and noise should be useful for all vorticity-based applications. The spatial averaging scale of the vorticity calculation is very easily adjusted from the native grid spacing (ringsize 4) up to an arbitrarily large size within the observational swath. This versatility makes it easy for a spatial scale to be chosen to match the needs of the application, or for a range of spatial scales to be considered. In the case of tropical disturbances, the range of spatial scales is highly useful for the identification of circulations when there is a great deal of serious rain contamination.

The error characteristics of the area averaged vorticity calculation can be described in terms of three types of errors: random observational error, truncation error associated with linear interpolation between wind vectors and mismatches in the spatial averaging scale (representation errors). The random observational error can be characterized in terms of an isotropic random vector error, with the number of observations defining the perimeter of the area and size of the area. This random error has a standard deviation that is approximately proportional to the random vector error, the radius of the area raised to the -1.5 power and grid spacing to the 0.5 power. That is, larger areas decrease the random error and finer grid spacing along the perimeter increases the number of data points and hence, increases the random error. It also appears that ambiguity selection errors are adequately described by the random vector component errors and do not need to be considered as an additional source of uncertainty.

Truncation errors are based upon the linear interpolation between grid points along the perimeter of the ring. The uncertainty in the truncation error is proportional to the square of the distance over which the interpolation occurs; therefore, the larger the distance between valid observations (non-missing and non-rain contamination flagged wind vectors), the larger the error. However, through the use of tropical storm composites, as provided by Minter et al.

(2007), the lower limit of random error is approximately 10^{-7} s^{-1} . It is impossible at this time to determine truncation error for real world examples due to limited data sources; however, it is substantially larger than this estimate.

Representation errors result in a negative bias (underestimation) when sampling cyclonic systems. This bias is substantial in comparison to the vorticity thresholds used in the Sharp et al. (2002) and Gierach et al. (2007) techniques. These thresholds are empirically chosen to match the spatial smoothing with the study's objective. For other applications, the threshold will likely need to be adjusted to account for the differences in smoothing in the techniques for calculating vorticity, particularly if the spatial scale (ringsize) is adjusted. This problem is of reduced importance for the application of tropical disturbances. Stronger, more intense systems (i.e., TDs and higher) tend to be more organized and have larger vorticities than smaller scale systems.

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BIOGRAPHICAL SKETCH

Kelly Ann McBeth was born in 1983 in Baltimore, MD to Carol and John McBeth. Kelly has one older sister, Melinda, who is pursuing a law degree from The Florida Coastal School of Law in Jacksonville, FL. Kelly's parents currently reside in Maryland. Kelly grew up in MD until pulling up roots to move to Florida for college. Kelly has always had a passion for weather and yearned to understand it.

Kelly graduated with honors from River Hill High School in June of 2001. Next, she went on to pursue her Bachelors of Science degree in Meteorology at The Florida State University in Tallahassee, FL and graduated in May of 2005. Knowing that there was still so much more to learn, Kelly applied and was accepted to the Masters program of the Meteorology Department at FSU. She served as a Teaching Assistant to Professors Ahlquist, Reasor and Ruscher. She was assigned her own Introduction to Meteorology Lab with seventeen undergraduate students and was responsible for generating and administering lab assignments, quizzes and homework. Kelly transitioned into a Research Assistant position at The Center for Ocean-Atmospheric Prediction Studies (COAPS) beginning in the spring of 2006, where she initiated her research under the guidance and supervision of Dr. Mark A. Bourassa.

Kelly has participated in three "blitz builds" with Dreambuilders for Habitat for Humanity in Belen, New Mexico and Biloxi, Mississippi and has plans to continue building Habitat homes for families in need. Kelly currently resides in Tallahassee, FL, accompanied by her new husband, John, and faithful cat, Nimbus.